

Generating Checking Sequences: When Resetting is not an Option

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2 Agenda

- ▶ Goals
 - ▶ To present the main concept of checking sequence generation
 - ▶ To present recent methods
 - ▶ To demonstrate why those methods work
 - ▶ To point future research
- ▶ Public
 - ▶ Newcomers to the area
 - ▶ Intuition over formulae
 - ▶ New PhD students

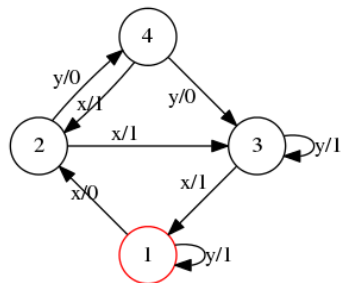
3 Model Based Testing

- ▶ Test Generation is Always Model-Based
 - ▶ Implicit models
 - ▶ System Understanding
 - ▶ Explicit models
 - ▶ Diagrams
 - ▶ State Machines

4 State Machines

- ▶ Simplest explicit models
 - ▶ Vanilla models
 - ▶ Understandable for non-experts
 - ▶ Semantic is the model itself

5 Finite State Machine



- ▶ It can be seen as
 - ▶ A regular language over pairs of input and outputs
 - ▶ A function from inputs sequences to output sequences

6 Test from State Machines

- ▶ Given a specification FSM
- ▶ Given an implementation
 - ▶ As a black-box
 - ▶ Only output sequences (in response to input sequences) are observable
- ▶ Is the implementation correct?
 - ▶ Does it behave accordingly?
 - ▶ Does it represent the same function?
 - ▶ Or an equivalent one (in some sense)?

7 Test from State Machines (II)

- ▶ Is it even possible to answer that?
 - ▶ A failed test is a negative answer
- ▶ For a positive answer
 - ▶ Is a finite test enough?

8 Testing Hypothesis

- ▶ Enter testing hypothesis
 - ▶ Without assumptions, the problem is unsolvable
 - ▶ With too many assumptions, the problem is trivial
 - ▶ With the right assumptions, the problem is interesting

9 Testing Hypothesis (II)

- ▶ **Modelling assumption**
 - ▶ The implementation can be modelled as an (unknown) FSM
 - ▶ Big assumption
 - ▶ Reduces the complexity of knowing how to test
- ▶ **Input Compatibility**
 - ▶ The implementation accepts the same inputs as the specification

10 Testing Hypothesis (III)

- ▶ **Boundness**
 - ▶ There is a known upper bound on the number of state in the unknown FSM
 - ▶ This is the most disputable one!
- ▶ **Determinism**
 - ▶ Always the same answer to a given input sequence
 - ▶ Verifiable in the specification
 - ▶ Assumed in the implementation

11 Checking experiments

- ▶ A set of input sequences (with corresponding output sequences) which identify uniquely the specification
 - ▶ Resets are used to bring the specification and the implementation the initial state
 - ▶ It is assumed to be reliable in the implementation
 - ▶ Yet another assumption

12 Checking experiments

▶ Generation Methods

- ▶ W^1
- ▶ Wp^2
- ▶ HSI^3

¹T. S. Chow. “Testing Software Design Modeled by Finite-State-Machines”. In: *IEEE Transactions on Software Engineering* 4.3 (May 1978), pp. 178–186.

²Susumu Fujiwara et al. “Test Selection Based on Finite State Models”. In: *IEEE Trans. Software Eng.* 17.6 (1991), pp. 591–603.

³N. Yevtushenko and A. Petrenko. “Synthesis of test experiments in some classes of automata”. In: *Automatic Control and Computer Sciences* 24.4 (1990), pp. 50–55.

13 Checking experiments (II)

- ▶ Generation Methods
 - ▶ H⁴
 - ▶ SPY⁵

⁴Rita Dorofeeva, Khaled El-Fakih, and Nina Yevtushenko. “An Improved Conformance Testing Method”. In: *Formal Techniques for Networked and Distributed Systems - FORTE 2005, 25th IFIP WG 6.1 International Conference, Taipei, Taiwan, October 2-5, 2005, Proceedings*. 2005, pp. 204–218.

⁵Adenilso Simao, Alexandre Petrenko, and Nina Yevtushenko. “Generating Reduced Tests for FSMs with Extra States”. In: *Testing of Software and Communication Systems, 21st IFIP WG 6.1 International Conference, TESTCOM 2009 and 9th International Workshop, FATES 2009, Eindhoven, The Netherlands, November 2-4, 2009. Proceedings*. 2009, pp. 129–145.

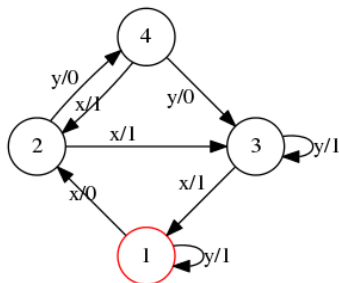
14 Checking experiments (III)

- ▶ Test Cases from HSI Method
 - ▶ {xxxx, xxyx, xxyy, xyxxy, xyxy, xyyx, xyyy, yx}
 - ▶ Length 39
- ▶ Test Cases from SPY Method
 - ▶ {xxxx, xxyx, xyxxyy, xyxyyy, xyyx, yx}
 - ▶ Length 32

15 Checking sequence

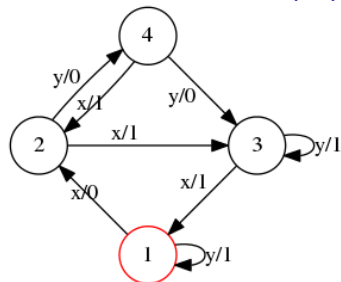
- ▶ A checking experiment with a single input sequence
 - ▶ No resets required
 - ▶ Strongly connected

16 Generation Methods



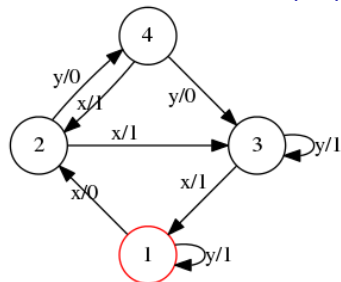
- ▶ Assume the FSM
- ▶ Assume the implementation can be modeled as an FSM with same input alphabet and at most 4 states

18 Generation Methods (III)



- ▶ Consider the input sequence
 - ▶ $\omega = yxyxyxyxyxyxyxyxyxyxyxyxyxyxyxyx$
 - ▶ Length 27
- ▶ The output sequence is
 - ▶ $\mu = 100101001101111011111100011$
- ▶ There is only one (out of more than 16 millions) FSM with at most 4 states, which answer ω with μ
 - ▶ There are possible renamed FSMs

19 Generation Methods (IV)



- ▶ Consider the input sequence

- ▶ $\omega' =$

xyyyxxxxxyxyxxyxyxxxxyxxxxyyyxyyyxyyyxyxyxyyyyxyyxxyyxxxyyyxxxyyx

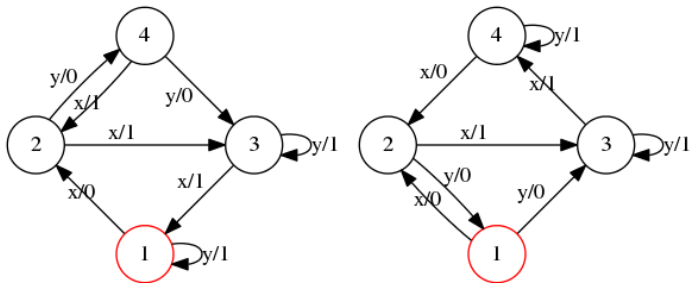
- ▶ Length 58

- ▶ The output sequence is

- ▶ $\mu' =$

00011011110111101111011111000111000110001111101111000100010

20 Generation Methods (V)



- ▶ Consider the input sequence

- ▶ $\omega' =$

xyyyxxxxyxyxxxxyxxxxyxyyyxyyyxyyyxyxyyyyxyyxxxxyyxxxxyyxx

- ▶ The output sequence is

- ▶ $\mu' =$

0001101111011110111011111000111000110001111101111000100010

21 Checking Sequence

- ▶ What is a checking sequence after all
 - ▶ Given a specification FSM
 - ▶ An input sequence (with the respective output sequence) which identifies uniquely (up to isomorphism) this FSM among a set of candidate FSMs
- ▶ The candidate FSMs
 - ▶ Set of FSMs with at most as many states as the specification FSM
 - ▶ The fault domain

22 Using a Checking Sequence

- ▶ Given a checking sequence
- ▶ Given a black-box implementation
- ▶ Assuming the implementation can be modeled by an FSM from the fault domain
- ▶ If the implementation passes the test (i.e., it produces the expected output)
 - ▶ The implementation is correct

23 Generating Checking Sequences

- ▶ Long tradition
 - ▶ Moore, 1958⁶
 - ▶ The seminal paper
 - ▶ The problem is set here

⁶Edward F. Moore. “Gedanken-Experiments on Sequential Machines”. In: *J. Symbolic Logic* 23.1 (1958).

24 Generating Checking Sequences (II)

- ▶ Long tradition
 - ▶ Hennie, 1965⁷
 - ▶ Generating checking sequences
 - ▶ The method is quite good, but not very algorithmic

⁷F. C. Hennie. “Fault-detecting experiments for sequential circuits”. In: *Proceedings of Fifth Annual Symposium on Circuit Theory and Logical Design*, 1965, pp. 95–110.

25 Generating Checking Sequences (III)

- ▶ Long tradition
 - ▶ Gonenc, 1970⁸
 - ▶ An algorithmic method
 - ▶ Let us have a look

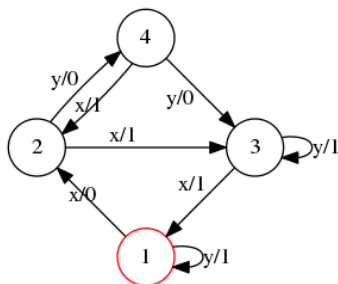
⁸G. Gonenc. “A method for the design of fault detection experiments”. In: *IEEE Transactions on Computers* 19 (1970), pp. 551–558.

26 Distinguishing States

- ▶ A way to distinguish all states of the FSMs⁹
- ▶ Distinguishing Sequence
 - ▶ Preset
 - ▶ An input sequence
 - ▶ Adaptive
 - ▶ An decision tree (nodes are inputs, edges are outputs)
- ▶ Distinguishing Set
 - ▶ A preset set of sequences, which common prefixes
 - ▶ Equivalent to an Adaptive Distinguishing Sequence

⁹David Lee and Mihalis Yannakakis. “Testing Finite-State Machines: State Identification and Verification”. In: *IEEE Trans. Computers* 43.3 (1994), pp. 306–320.

27 Distinguishing States (II)



- ▶ Preset Distinguishing Sequence
- ▶ $X_d = yxy$
 - ▶ State 1 answers with 100
 - ▶ State 2 answers with 010
 - ▶ State 3 answers with 111
 - ▶ State 4 answers with 011

28 Distinguishing States (III)

▶ Insights

- ▶ X_d can be used to identify a unknown state of the machine
- ▶ X_d can be used to confirm that the machine is in a given state
- ▶ If X_d is applied to every state of the specification and the implementation
- ▶ If the implementation answers as the specification
 - ▶ Then, the implementation has at least 4 states
 - ▶ X_d is a preset distinguishing sequence for the implementation

29 Distinguishing States (IV)

- ▶ Insights
 - ▶ $X_d X_d$ can be used to confirm the state reached by the first application of X_d
 - ▶ If $X_d X_d$ is applied in each state
 - ▶ Then, we can identify which state the implementation is in

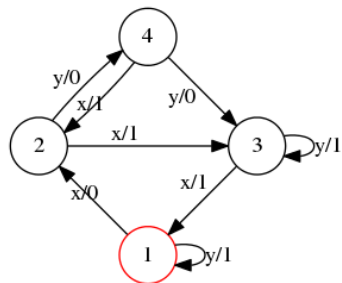
30 Distinguishing States (V)

- ▶ Insights
 - ▶ For a given transition from a (known) state with a given input
 - ▶ X_d can be used to confirm that the reached state is correct

31 Generating a Checking Sequence

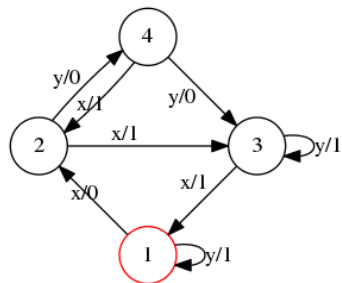
- ▶ α -sequences
 - ▶ Recognizing states
- ▶ β -sequences
 - ▶ Confirming transitions
- ▶ T -sequences (transfer sequences)
 - ▶ Bridging from one state to another
 - ▶ Gluing the sequences
 - ▶ Avoiding circularity in the assumptions

32 Generating a Checking Sequence (II)



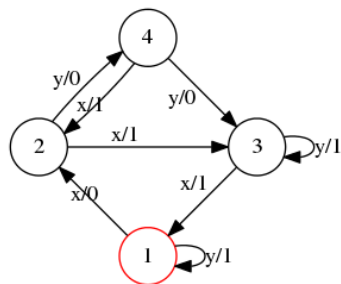
- ▶ Consider the sequence
 - ▶ $X_d X_d X_d = yxyyxyxy$ from state 1
 - ▶ with outputs $y.1 \ x.0 \ y.0 \ y.0 \ x.1 \ y.1 \ y.1 \ x.0 \ y.0$

33 Generating a Checking Sequence (III)



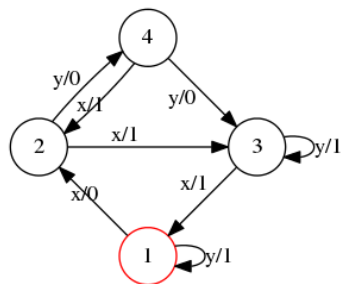
- ▶ Consider the sequence
 - ▶ $X_d X_d X_d = yxyyxyxy$ from state 1
 - ▶ with outputs [1]y.1 x.0 y.0 [4]y.0 x.1 y.1 [1]y.1 x.0 y.0

34 Generating a Checking Sequence (IV)



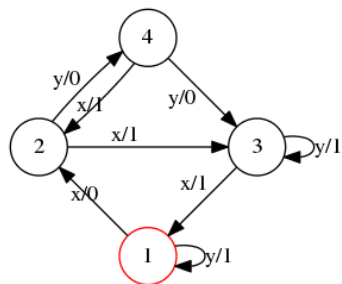
- ▶ Consider the sequence
 - ▶ $X_d X_d X_d = yx y y x y y x y$ from state 1
 - ▶ with outputs [1]y.1 x.0 y.0 [4]y.0 x.1 y.1 [1]y.1 x.0 y.0 (4)
 - ▶ This is a α -sequence $(1, X_d X_d X_d)$

35 Generating a Checking Sequence (V)



- ▶ Consider the sequence
 - ▶ $X_d X_d = yx y y x y$ from state 2
 - ▶ with outputs [2] y.0 x.1 y.0 [4] y.0 x.1 y.1 (4)
 - ▶ This is another α -sequence $(2, X_d X_d)$

36 Generating a Checking Sequence (VI)



- ▶ Consider the sequence
 - ▶ $X_d X_d = yxyyxy$ from state 3
 - ▶ with outputs [3] y.1 x.1 y.1 [1] y.1 x.0 y.0 (4)
 - ▶ This is another α -sequence

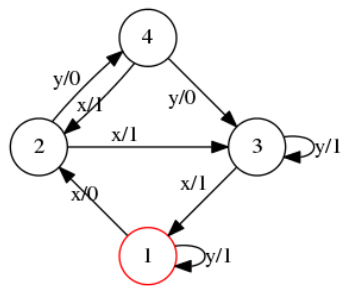
37 Generating a Checking Sequence (VII)

- ▶ The alpha set is the set of α -sequences, marked with the respective starting states
 - ▶ There are three $(1, X_d X_d X_d), (2, X_d X_d), (3, X_d X_d)$

38 Generating a Checking Sequence (VIII)

- ▶ The β -sequences are generated per transition
 - ▶ Consider the transition $(1, x)$
 - ▶ The corresponding β -sequence is $xX_d = (1)x.0[2]y.0x.1y.0(4)$
 - ▶ Actually $(1, xX_d)$
 - ▶ There are, then, eight β -sequences, one for each transitions

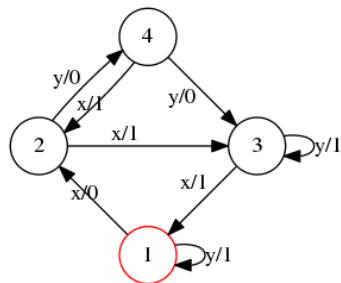
39 Generating a Checking Sequence (IX)



▶ Testing fragments

- ▶ $(1, X_d X_d X_d, 4), (2, X_d X_d, 4), (3, X_d X_d, 4)$
- ▶ $(1, x X_d, 4), (1, y X_d, 4), (2, x X_d, 1), (2, y X_d, 1), (3, x X_d, 4), (3, y X_d, 1), (4, x X_d, 4), (4, y X_d, 1)$

40 Generating a Checking Sequence (X)



► Gluing them

- Using transfer sequences (T -sequences) if needed
 - Avoid circularity
- $(1, X_d X_d X_d, 4)$ $(4, x, 2)$ $(2, X_d X_d, 4)$ $(4, y, 3)$ $(3, X_d X_d, 4)$ $(4, x X_d, 4)$
 $(4, y X_d, 1)$ $(1, y X_d, 4)$ $(4, x, 2)$ $(2, x X_d, 1)$ $(1, x X_d, 4)$ $(4, x, 2)$
 $(2, y X_d, 1)$ $(1, xx, 3)$ $(3, x X_d, 4)$ $(4, y, 3)$ $(3, y X_d, 1)$

41 Generating a Checking Sequence (XI)

- ▶ Extracting the checking sequence

- ▶ $X_d X_d X_d x X_d X_d y X_d X_d x X_d y X_d y X_d x x X_d x X_d x y X_d x x x X_d y y X_d$
- ▶ $y x y y x y y x y x y y x y y y x y y x y x y x y y y x y y y x y x x y x y x y x y y x y x x x y x y y y x y$
 - ▶ Length 60

42 Generating a Checking Sequence (XII)

- ▶ Optimizing T -sequences¹⁰
 - ▶ Generating a graph with α -, β - and (sort of) T -sequences
 - ▶ Find the shortest sequence with all α - and β -sequences
 - ▶ T -sequences are optional
 - ▶ Rural Chinese Postman Problem (RCPP)¹¹
 - ▶ In the best scenario, no T -sequences.
 - ▶ The shortest possible with this approach is of length 53

¹⁰H. Ural, X. Wu, and F. Zhang. “On minimizing the lengths of checking sequences”. In: *IEEE Transactions on Computers* 46.1 (1997), pp. 93–99.

¹¹R. M. Hierons and H. Ural. “Optimizing the length of checking sequences”. In: *IEEE Transactions on Computers* 55.5 (2006), pp. 618–629.

43 Local Optimization Method

- ▶ Greedy approach¹²
- ▶ Until all transitions are verified
 - ▶ (Case 1) the current state is not recognized
 - ▶ Apply the distinguishing sequence for that state
 - ▶ (Case 2) the current state is recognized and there is a non-verified input at the end state
 - ▶ Apply the input plus the distinguishing sequence
 - ▶ (Case 3) the current state is recognized and all inputs are verified at the end state
 - ▶ Transfer to a state with non-verified input, using only verified transitions

¹²Adenilso Simao and Alexandre Petrenko. “Generating Checking Sequences for Partial Reduced Finite State Machines”. In: *Testing of Software and Communicating Systems, 20th IFIP TC 6/WG 6.1 International Conference, TestCom 2008, 8th International Workshop, FATES 2008, Tokyo, Japan, June 10-13, 2008, Proceedings*. 2008, pp. 153–168.

44 Local Optimization Method (II)

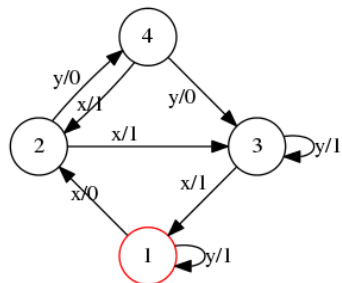
▶ Insights

- ▶ Sometimes it is possible to use shorter sequence to distinguish
 - ▶ As in¹³
- ▶ Sometimes a transition is verified indirectly
 - ▶ As in¹⁴

¹³Hasan Ural and Fan Zhang. “Reducing the Lengths of Checking Sequences by Overlapping”. In: *Testing of Communicating Systems, 18th IFIP TC6/WG6.1 International Conference, TestCom 2006, New York, NY, USA, May 16-18, 2006, Proceedings*. 2006, pp. 274–288.

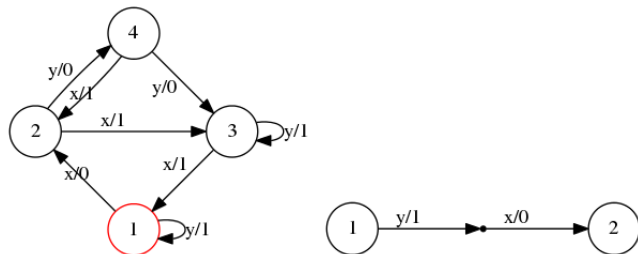
¹⁴Jessica Chen et al. “Eliminating Redundant Tests in a Checking Sequence”. In: *Testing of Communicating Systems, 17th IFIP TC6/WG 6.1 International Conference, TestCom 2005, Montreal, Canada, May 31 - June 2, 2005, Proceedings*. 2005, pp. 146–158.

45 Local Optimization Method (III)



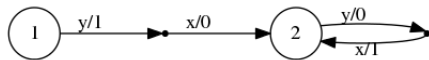
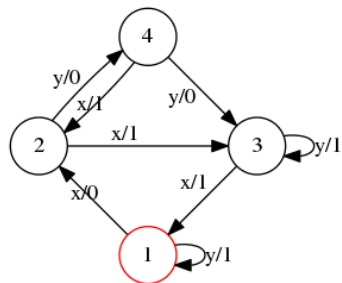
- ▶ $X_d^1 = y.1x.0$
- ▶ $X_d^2 = y.0x.1y.0$
- ▶ $X_d^3 = y.1x.1$
- ▶ $X_d^4 = y.0x.1y.1$

46 Local Optimization Method (IV)



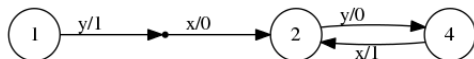
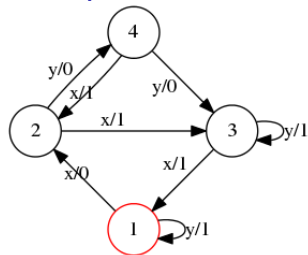
- ▶ We start applying X_d
 - ▶ $\omega = [1]y.1x.0$
- ▶ We apply X_d again
 - ▶ $\omega = [1]y.1x.0[2]y.0x.1y.0$
 - ▶ The fragment $(1, yx, 2)$ is verified

47 Local Optimization Method (V)



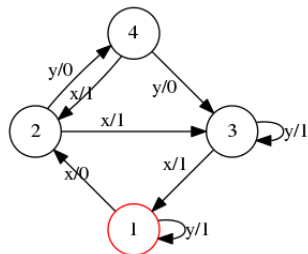
- ▶ We apply X_d again, but using the fact that a suffix of ω is a prefix of X_d
 - ▶ $\omega = [1]y.1x.0[2]y.0x.1[2]y.0x.1y.0$
 - ▶ The fragment $(2, yx, 2)$ is verified
 - ▶ Then
 - ▶ $\omega = [1]y.1x.0[2]y.0x.1[2]y.0x.1[2]y.0$

48 Local Optimization Method (VI)



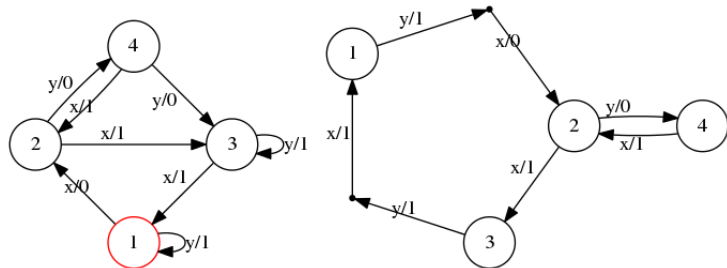
- ▶ We apply X_d again
 - ▶ This time, there is no point in reusing the suffix
 - ▶ $\omega = [1]y.1x.0[2]y.0x.1[2]y.0x.1[2]y.0[4]y.0x.1y.1$
 - ▶ The fragment $(2, y, 4)$ is verified
 - ▶ It is the transition $(2, y)$
 - ▶ As fragments $(2, yx, 2)$ and $(2, y, 4)$ are verified, so is $(4, x, 2)$
 - ▶ Another transition is verified: $(4, x)$
 - ▶ $\omega = [1]y.1x.0[2]y.0(4)x.1[2]y.0(4)x.1[2]y.0[4]y.0x.1y.1$

49 Local Optimization Method (VII)



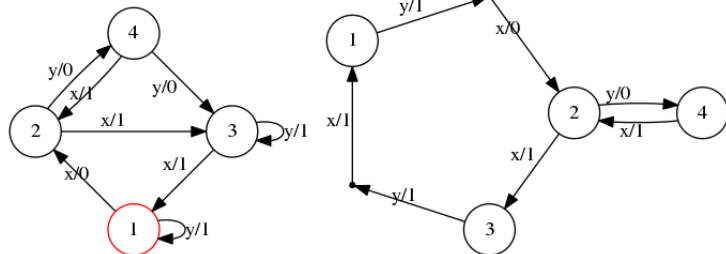
- ▶ We apply X_d again
 - ▶ $\omega = [1]y.1x.0[2]...[4]y.0x.1[1]y.1x.0[2]$
 - ▶ Since $(1, yx, 2)$ is verified

50 Local Optimization Method (VIII)



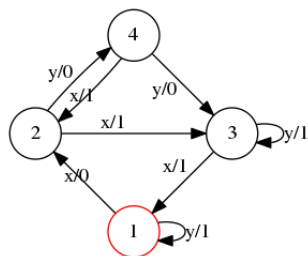
- ▶ There is an unverified transition in state 2, name $(2, x)$
 - ▶ Then, apply input x , followed by the X_d
 - ▶ $\omega = [1]y.1x.0[2]...[4]y.0x.1[1]y.1x.0[2]x.1[3]y.1x.1$
 - ▶ The fragment $(2, x, 3)$ is verified
 - ▶ Transition $(2, x)$ is verified

51 Local Optimization Method (IX)



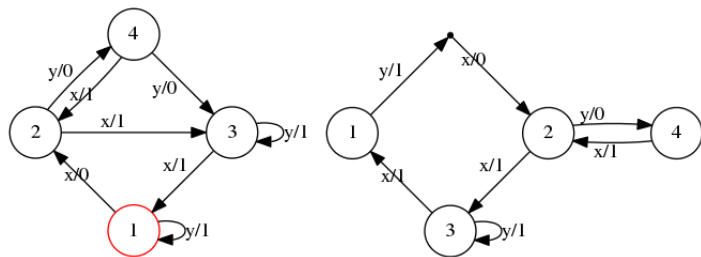
- ▶ We apply X_d
 - ▶ $\omega = [1]y.1x.0[2]...[2]x.1[3]y.1x.1[1]y.1x.0[2]$
 - ▶ Since $(1, yx, 2)$ is verified
 - ▶ The fragment $(3, yx, 1)$ is verified

52 Local Optimization Method (X)



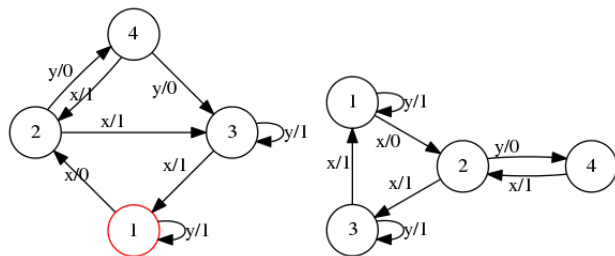
- ▶ There is no unverified transition from state 2
 - ▶ Transfer to a state where there is
 - ▶ Using only verified transitions
 - ▶ $\omega = [1]y.1x.0[2] \dots [1]y.1x.0[2]x.1[3]$
 - ▶ Since $(2, x, 3)$ is verified

53 Local Optimization Method (XI)



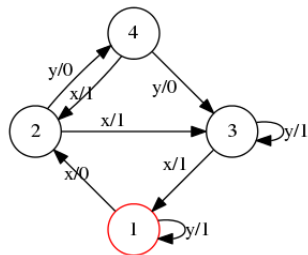
- ▶ Verify transitions either $(3, x)$ or $(3, y)$
 - ▶ Let us choose $(3, y)$
 - ▶ Apply y , then X_d
- ▶ $\omega = [1]y.1x.0[2]...[1]y.1x.0[2]x.1[3]y.1[3]y.1(3)x.1[1]$
 - ▶ The fragment $(3, y, 3)$ is verified
 - ▶ So are transitions $(3, y)$ and $(3, x)$

54 Local Optimization Method (XII)



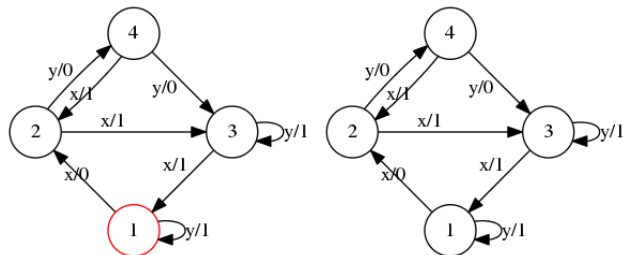
- ▶ Verify transitions either $(1, x)$ or $(1, y)$
 - ▶ Let us choose $(1, y)$
 - ▶ Apply y , then X_d
- ▶ $\omega = [1]y.1x.0[2]...[3]y.1[3]x.1[1]y.1[1]y.1(1)x.0[2]$

55 Local Optimization Method (XIII)



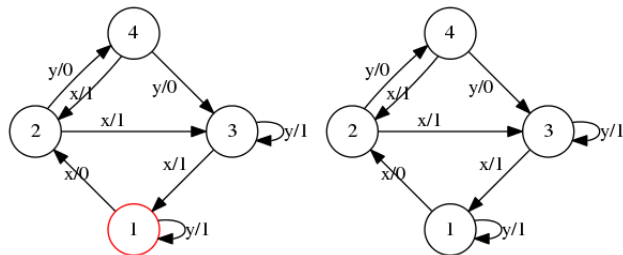
- ▶ There is no unverified transition from state 2
 - ▶ Transfer to a state where there is
 - ▶ $\omega = [1]y.1x.0[2] \dots [1]y.1(1)x.0[2]y.0[4]$
 - ▶ Since $(2, y, 4)$ is verified

56 Local Optimization Method (XIV)



- ▶ Verify transitions (4, y)
 - ▶ Apply y, then X_d
- ▶ $\omega = [1]y.1x.0[2]...[2]y.0[4]y.0[3]y.1x.1$

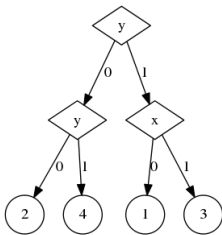
57 Local Optimization Method (XV)



- ▶ $\omega = yxyxyxyyyxyxxxyxyxxxyxyyyxyyyx$
- ▶ Length 27

58 Distinguishing Set

- ▶ One sequence for each state
- ▶ For each pair of states, there exists a common prefix of both corresponding sequences which separates them
 - ▶ $X_d^1 = y.1x.0$
 - ▶ $X_d^2 = y.0y.0$
 - ▶ $X_d^3 = y.1x.1$
 - ▶ $X_d^4 = y.0y.1$



- ▶ Adaptive Distinguishing Sequence

59 Distinguishing Set (II)

- ▶ A shorter checking sequence (in some cases)
- ▶ In the running example
 - ▶ $\omega = yxyyyxyxxxyxyxxxyxyxyxy$
 - ▶ Length 23

60 Without Distinguishing Sequence

- ▶ A characterization set¹⁵
- ▶ A set of sequences
 - ▶ For each pair of states, there exists a sequence which separates them
 - ▶ Always available for minimal machines

¹⁵T. S. Chow. "Testing Software Design Modeled by Finite-State-Machines". In: *IEEE Transactions on Software Engineering* 4.3 (May 1978), pp. 178–186.

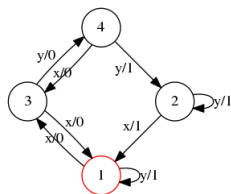
61 Without Distinguishing Sequence (II)

- ▶ The set of sequence should be applied to same state of the implementation
 - ▶ Signature
- ▶ How to return to the same state in the implementation?
 - ▶ Locating sequence^{16, 17}

¹⁶F. C. Hennie. “Fault-detecting experiments for sequential circuits”. In: *Proceedings of Fifth Annual Symposium on Circuit Theory and Logical Design*. 1965, pp. 95–110.

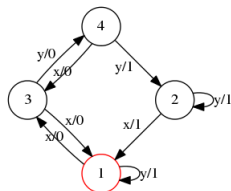
¹⁷Ali Rezaki and Hasan Ural. “Construction of checking sequences based on characterization sets”. In: *Computer Communications* 18.12 (1995), pp. 911–920.

62 Without Distinguishing Sequence (III)



- ▶ Characterization set
 - ▶ $W = \{x, yx\}$
- ▶ Suppose we are at state s we suspect to be 2
 - ▶ Apply yx observing 11
 - ▶ It can be state 4 instead
- ▶ How to come back to s to apply x ?

63 Without Distinguishing Sequence (IV)



- ▶ Repeating yx many times
 - ▶ We do the following
 - ▶ $L_2 = s_1 yx xyy s_2 yx xyy s_3 yx xyy s_4 yx xyy s_5 yx xyy s_6 x$
 - ▶ $yxxyy$ cycles from state 2 back to state 2, in the specification

64 Without Distinguishing Sequence (V)

- ▶ $L_2 = s_1 yx xyy s_2 yx xyy s_3 yx xyy s_4 yx xyy s_5 yx xyy s_6 x$
 - ▶ As there are 4 states
 - ▶ Two of the states in the set $\{s_1, s_2, s_3, s_4, s_5\}$ should be the same
 - ▶ Then, s_6 should be one of the states $\{s_1, s_2, s_3, s_4\}$ for which we know the answer for yx
 - ▶ We then can infer which state it is, from the answers for yx and x

65 Without Distinguishing Sequence (VI)

- ▶ $L_2 = yxxyyyxyyyxyyyxyyyxyy[2]x$
 - ▶ L_2 is a locating sequence for state 2
- ▶ $L_1 = yxyxyxyxyxyx[1]x$
 - ▶ L_1 is a locating sequence for state 1
- ▶ $L_3 = yxyxyxyx[3]x$
 - ▶ L_3 is a locating sequence for state 3
- ▶ $L_4 = yxxyyxyxyxyxyxy[4]x$
 - ▶ L_4 is a locating sequence for state 4

66 Without Distinguishing Sequence (VII)

- ▶ Apply all locating sequences
 - ▶ It should be done first
- ▶ Suppose we would like to check the end state after an input sequence α after state 4
- ▶ Apply $L_2 T_4 \alpha y x$ and $L_2 T_4 \alpha x$
 - ▶ T_4 transfer to state 4 in the specification

67 Sufficient Conditions

- ▶ Why the method work
 - ▶ A framework for proving correctness

68 Sufficient Conditions (II)

- ▶ Confirmed Sequences
 - ▶ When it is possible to be sure in which state the implementation is at
- ▶ Convergence (and Divergence)
 - ▶ When it is possible to be sure that two sequences reach the same state (or distinct states)

69 Sufficient Conditions (III)

- ▶ Consider the sequence
 - ▶ $xyyxyxyxyxyxyxyx$
 - ▶ Length 17
- ▶ It is a checking sequence
 - ▶ It can be proved by using the sufficient conditions
 - ▶ Theorems and Lemmas in¹⁸

¹⁸Adenilso Simao and Alexandre Petrenko. "Checking Completeness of Tests for Finite State Machines". In: *IEEE Transactions on Computers* 59 (2010), pp. 1023–1032.

70 Sufficient Conditions (IV)

- ▶ Adding the outputs
 - ▶ $x_0 y_0 y_0 x_1 y_1 x_0 x_1 y_1 x_1 y_1 x_0 y_0 x_1 y_0 y_0 y_1 x_1$

71 Sufficient Conditions (IV)

- ▶ Adding the outputs
 - ▶ $x_0 y_0 y_0 x_1 y_1 x_0 x_1 y_1 x_1 y_1 x_0 y_0 x_1 y_0 y_0 y_1 x_1$

72 Sufficient Conditions (IV)

- ▶ Adding the outputs
 - ▶ $x_0y_0y_0x_1y_1x_0x_1y_1x_1y_1x_0y_0x_1y_0y_0y_1x_1$
- ▶ Identifying 4 states which cannot be the same in any implementation passing the test
 - ▶ $x_0y_0y_0x_1y_1x_0x_1y_1x_1y_1x_0y_0x_1y_0y_0y_1x_1$
 - ▶ Finding an n -clique in an n -partite graph!
 - ▶ NP-Complete

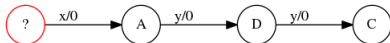
73 Sufficient Conditions (V)

- ▶ Marking them

- ▶ $x_0Ay_0y_0x_1By_1x_0x_1Cy_1x_1y_1x_0y_0x_1y_0Dy_0y_1x_1$

74 Sufficient Conditions (VI)

- ▶ Finding states which cannot be three of them
 - ▶ $?x0Ay0?y0?x1By1?x0?x1Cy1?x1?y1?x0?y0?x1?y0Dy0?y1?x1?$
- ▶ Marking them with the only one it can be
 - ▶ $?x0Ay0?y0?x1By1?x0?x1Cy1?x1By1?x0?y0?x1?y0Dy0?y1?x1?$
 - ▶ $?x0Ay0?y0?x1By1?x0?x1Cy1?x1By1?x0?y0?x1Ay0Dy0?y1?x1?$
 - ▶ $?x0Ay0?y0?x1By1?x0?x1Cy1?x1By1?x0?y0?x1Ay0Dy0Cy1?x1?$



75 Sufficient Conditions (VII)

- ▶ How about this state?
 - ▶ $?x_0Ay_0?y_0?x_1By_1?x_0?x_1Cy_1?x_1By_1?x_0?y_0?x_1Ay_0Dy_0Cy_1?x_1?$
 - ▶ Either A or D

76 Sufficient Conditions (VIII)

- ▶ As the implementation is deterministic, if two points are the same state, the common suffixes lead to the same state
 - ▶ ?x0Ay0?y0?x1By1?x0?x1Cy1?x1By1?x0?y0?x1Ay0Dy0Cy1?x1?
 - ▶ ?x0Ay0Dy0Cx1By1?x0?x1Cy1?x1By1?x0?y0?x1Ay0Dy0Cy1?x1?
 - ▶ ?x0Ay0Dy0Cx1By1?x0?x1Cy1?x1By1?x0?y0?x1Ay0Dy0Cy1?x1?



77 Sufficient Conditions (IX)

- ▶ We now that the previous state cannot be D

- ▶ $?x0Ay0Dy0Cx1By1?x0?x1Cy1?x1By1?x0?y0?x1Ay0Dy0Cy1?x1?$
- ▶ $?x0Ay0Dy0Cx1By1?x0?x1Cy1?x1By1?x0Ay0?x1Ay0Dy0Cy1?x1?$



78 Sufficient Conditions (X)

► Common suffixes again

► ?x0Ay0Dy0Cx1By1?x0?x1Cy1?x1By1?x0Ay0?x1Ay0Dy0Cy1?x1?

►

?x0Ay0Dy0Cx1By1?x0?x1Cy1?x1By1?x0Ay0Dx1Ay0Dy0Cy1?x1?



79 Sufficient Conditions (XI)

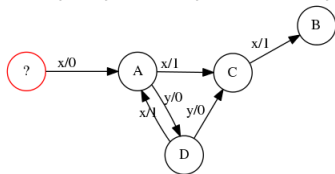
- ▶ Common suffixes again



?x0Ay0Dy0Cx1By1?x0?x1Cy1?x1By1?x0Ay0Dx1Ay0Dy0Cy1?x1?



?x0Ay0Dy0Cx1By1?x0Ax1Cy1?x1By1?x0Ay0Dx1Ay0Dy0Cy1?x1?



80 Sufficient Conditions (XII)

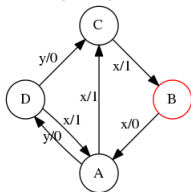
- ▶ We can infer the initial state now



?x0Ay0Dy0Cx1By1?x0Ax1Cy1?x1By1?x0Ay0Dx1Ay0Dy0Cy1?x1?



Bx0Ay0Dy0Cx1By1?x0Ax1Cy1?x1By1?x0Ay0Dx1Ay0Dy0Cy1?x1?



81 Sufficient Conditions (XIII)

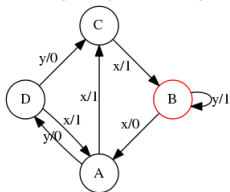
- ▶ We can also infer other states



$Bx0Ay0Dy0Cx1By1?x0Ax1Cy1?x1By1?x0Ay0Dx1Ay0Dy0Cy1?x1?$



$Bx0Ay0Dy0Cx1By1Bx0Ax1Cy1?x1By1?x0Ay0Dx1Ay0Dy0Cy1?x1?$



82 Sufficient Conditions (XIV)

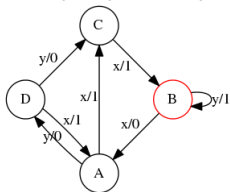
- ▶ We can also infer other states



$Bx0Ay0Dy0Cx1By1Bx0Ax1Cy1?x1By1?x0Ay0Dx1Ay0Dy0Cy1?x1?$



$Bx0Ay0Dy0Cx1By1Bx0Ax1Cy1?x1By1Bx0Ay0Dx1Ay0Dy0Cy1?x1?$



83 Sufficient Conditions (XV)

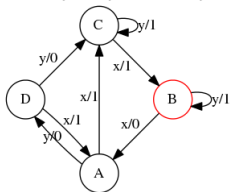
- ▶ We can also infer other states



$Bx0Ay0Dy0Cx1By1Bx0Ax1Cy1?x1By1Bx0Ay0Dx1Ay0Dy0Cy1?x1?$



$Bx0Ay0Dy0Cx1By1Bx0Ax1Cy1Cx1By1Bx0Ay0Dx1Ay0Dy0Cy1?x1?$

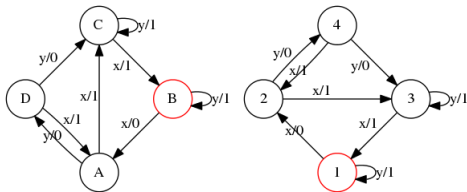


84 Sufficient Conditions (XVI)

- ▶ All transitions are inferred



$Bx0Ay0Dy0Cx1By1Bx0Ax1Cy1Cx1By1Bx0Ay0Dx1Ay0Dy0Cy1?x1?$



85 Sufficient Conditions (XVII)

- ▶ Thus, it is a checking sequence
 - ▶ $xyyxyxxyxyxyxyyyx$
 - ▶ Length 17
- ▶ It is very close to the shortest possible
 - ▶ $xyxyyyyyxyxxxx$
 - ▶ Length 14

86 Related work

- ▶ Extensions to the RCPP approach
 - ▶ Using adaptive distinguishing sequences¹⁹
 - ▶ Avoiding verifying some transitions²⁰
 - ▶ Allowing for overlapping²¹

¹⁹Robert M. Hierons et al. “Using adaptive distinguishing sequences in checking sequence constructions”. In: *Proceedings of the 2008 ACM Symposium on Applied Computing (SAC), Fortaleza, Ceara, Brazil, March 16-20, 2008*. 2008, pp. 682–687.

²⁰Jessica Chen et al. “Eliminating Redundant Tests in a Checking Sequence”. In: *Testing of Communicating Systems, 17th IFIP TC6/WG 6.1 International Conference, TestCom 2005, Montreal, Canada, May 31 - June 2, 2005, Proceedings*. 2005, pp. 146–158.

²¹Hasan Ural and Fan Zhang. “Reducing the Lengths of Checking Sequences by Overlapping”. In: *Testing of Communicating Systems, 18th IFIP TC6/WG6.1 International Conference, TestCom 2006, New York, NY, USA, May 16-18, 2006, Proceedings*. 2006, pp. 274–288.

87 Related work (II)

- ▶ Extension to greedy approach
 - ▶ Using UIOs²²
 - ▶ Dealing with non-deterministic machines²³

²²Adenilso Simao and Alexandre Petrenko. “Checking Sequence Generation Using State Distinguishing Subsequences”. In: *Second International Conference on Software Testing Verification and Validation, ICST 2009, Denver, Colorado, USA, April 1-4, 2009, Workshops Proceedings*. 2009, pp. 48–56.

²³Alexandre Petrenko, Adenilso Simao, and Nina Yevtushenko. “Generating Checking Sequences for Nondeterministic Finite State Machines”. In: *Fifth IEEE International Conference on Software Testing, Verification and Validation, ICST 2012, Montreal, QC, Canada, April 17-21, 2012*. 2012, pp. 310–319.

88 Related work (III)

► Recent work

- Generating good adaptive distinguishing sequences²⁴
- Removing (some) repetition in Locating Sequences²⁵
- Combining several distinguishing sequences²⁶

²⁴Uraz Cengiz Türker, Tonguç Ünlüyurt, and Hüsnü Yenigün. “Effective algorithms for constructing minimum cost adaptive distinguishing sequences”. In: *Information & Software Technology* 74 (2016), pp. 69–85.

²⁵Guy-Vincent Jourdan, Hasan Ural, and Hüsnü Yenigün. “Reducing locating sequences for testing from finite state machines”. In: *Proceedings of the 31st Annual ACM Symposium on Applied Computing, Pisa, Italy, April 4-8, 2016*. 2016, pp. 1654–1659.

²⁶Canan Güniçen, Guy-Vincent Jourdan, and Hüsnü Yenigün. “Using Multiple Adaptive Distinguishing Sequences for Checking Sequence Generation”. In: *Testing Software and Systems - 27th IFIP WG 6.1 International Conference, ICTSS 2015, Sharjah and Dubai, United Arab Emirates, November 23-25, 2015, Proceedings*. 2015, pp. 19–34.

89 Concluding Remarks

- ▶ Checking sequence
 - ▶ When resetting is not an option
- ▶ Long tradition
 - ▶ Old, but gold
- ▶ Not rocket science
- ▶ Still active

90 Concluding Remarks (II)

► Thank you! 😊

Generating Checking Sequences: When Resetting is not an Option

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